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# Toward Shared Working Space of Human and Robotic Agents through Dipole Flow Field for Dependable Path Planning

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## 2 ABSTRACT

3 Recent industrial developments in autonomous systems, or agents, which assume that humans  
4 and the agents share the same space or even work in close proximity, open for new challenges in  
5 robotics, especially in motion planning and control. In these settings, the control system should  
6 be able to provide these agents a reliable path following control when they are working in a group  
7 or in collaboration with one or several humans in complex and dynamic environments. In such  
8 scenarios, these agents are not only moving to reach their goals, i.e. locations, they are also  
9 aware of the movements of other entities to find a collision-free path. Thus, this paper proposes  
10 a dependable, i.e. safe, reliable and effective, path planning algorithm for a group of agents  
11 that share their working space with humans. Firstly, the method employs the Theta\* algorithm  
12 to initialise the paths from a starting point to a goal for a set of agents. As Theta\* algorithm is  
13 computationally heavy, it only reruns when there is a significant change of the environment. To  
14 deal with the movements of the agents, a static flow field along the configured path is defined. This  
15 field is used by the agents to navigate and reach their goals even if the planned trajectories are  
16 changed. Secondly, a dipole field is calculated to avoid the collision of agents with other agents  
17 and human subjects. In this approach, each agent is assumed to be a source of a magnetic  
18 dipole field in which the magnetic moment is aligned with the moving direction of the agent. The  
19 magnetic dipole-dipole interactions between these agents generate repulsive forces to help them  
20 to avoid collision. The effectiveness of the proposed approach has been evaluated with extensive  
21 simulations. The results show that the static flow field is able to drive agents to the goals with a  
22 small number of requirements to update the path of agents. Meanwhile, the dipole flow field plays  
23 an important role to prevent collisions. The combination of these two fields results in a safe path  
24 planning algorithm, with a deterministic outcome, to navigate agents to their desired goals.

25 **Keywords:** navigation field, Theta star algorithm, dependability, multiple agents, path planning, dynamic environment.

## 1 INTRODUCTION

26 Until recently, robots have played a critical role in the manufacturing industry where the automatic robots  
27 perform repetitive and sometimes heavy tasks. The majority of these solutions assume high precision  
28 with respect to movements and positioning of the robots, without relying on sensors, or at least extensive  
29 sensor feedback. However, technological advancements in recent years have resulted in a shift of attention  
30 from pre-programmed automatic solutions to (semi)-autonomous systems that can operate in unstructured  
31 environments, and even co-exist with humans. As a result of this shift, robots will be more involved in  
32 our daily activities. Thus, they will be allowed to have more interactions with humans, share working  
33 space with humans as well as make their own decisions with some accepted levels of uncertain information  
34 collected from the surrounding environment. For instance, there is a rise of interest in self-driving cars  
35 where the fully autonomous mode has been investigated to help drive the car in city centers, substandard  
36 roads or busy highways without causing accidents. In the health care domain, robots are assumed to assist  
37 elderly people in their daily activities. In this context, different levels of safety need to be taken into  
38 account, e.g. develop an autonomous control to avoid executing any movements that the users do not  
39 expect and also to prevent accident caused by a person being hit by the robot. The challenges, and the  
40 opportunities, in the health care domain becomes more evident considering care at home. Going back to  
41 the main application domain, i.e. industrial robotics, it is evident that the next generation solutions assume  
42 high degree of interaction and collaboration between mixed teams of humans and robots. Obviously, the  
43 approach taken by these solutions will not exclude today's standard solutions. Thus, it is most likely that  
44 different solutions will exist side by side in the near future.

45 Nevertheless, the developments in autonomous robots that co-existence of humans and robots, have  
46 opened new challenges in research areas of robotics, e.g., in motion planning and control. In particular, the  
47 control system should be able to provide the robots a reliable motion planning and control ability when  
48 the robots are working in a group or in collaboration with one or several humans in complex and dynamic  
49 environments. This means that the robots must meet certain requirements on trustworthiness/dependability  
50 in order to be allowed to work with humans. The dependability of a robotic agent is presented by main  
51 attributes including availability, i.e. the continuous operations of the system over a time interval, reliability,  
52 i.e. the ability of the system to provide correct services, and safety, i.e. the robotic agent must ensure safe  
53 controls to avoid any catastrophic consequences on users, other robots, and finally the environment. In  
54 order to implement a dependable robotic agent, important efforts have been attempted in several directions.  
55 Firstly, level of robot autonomy is automatically adaptive to the working context in order to address  
56 alternative complexities of environments. Secondly, the robot is willing to share the control with humans  
57 and other robots to optimise the working performance as well as to deal with complicated tasks that the  
58 robot cannot complete by itself. Lastly, to some extent, the robot must be able to handle the dynamic  
59 changes that occur in the environment, and to operate in accordance with the presence of other robots  
60 and humans in the same working space. This work mainly focuses on the last approach to enhance the  
61 robustness and dependability of the agents while working together with others and humans to complete a  
62 task.

63 Note also that, the high-level specification of a complicated movement of robots can be constructed  
64 through a sequence of lower level motion and path planning. A common problem is the movement of  
65 a robot arm, which can be composed of a sequence of trajectory planning and collision detection steps  
66 (Rubio et al., 2012, 2018). Therefore, motion and path planning are concerned as the basic, and separate,  
67 constructions for plans of robotic actions. Path planning is the process which is utilised to construct a  
68 collision-free path from a starting point to a destination given a full, partial or dynamic map. Motion

69 planning, meanwhile, is the progress in which a series of actions are needed to be defined to follow the  
70 planned path. The most common practice in robotics is to address the navigation problem using path  
71 planning, i.e. pure geometric planning from point to point, then motion planning is to realise the feasibility  
72 of the path. As the output of path planning will later determine the way to plan robots' motion, the path  
73 planing algorithm is better incorporated with motion planning to optimise the movement of the robot. This  
74 means that the path planning could be realised at every locations within the form of navigation field to  
75 make transformation from path to motion planning easier. Besides, the moving path must be estimated to  
76 avoid many changes of moving directions to save energy used to perform movements.

77 With regard to above mentioned issues, this paper addresses path planning of robotic agents in the context  
78 of shared working space of humans and agents. The aim is to develop a path planning algorithm to deal  
79 with the dynamic changes of environments and complicated maps with multiple static obstacles having  
80 a wide range of shapes. The algorithm also helps agents avoid collisions with humans and others in the  
81 shared environment, in which a group of agents are designed to collaborate with each in order to plan their  
82 optimal paths, in real-time. Finally, how to combine the aforementioned factors of motion planning into the  
83 developed path planning algorithm is investigated.

84 So far, numerous path planning approaches have been proposed to address control movement of robots.  
85 Most of them have been focused on searching to find a path from a starting point to a destination in  
86 either static or dynamic map. Meanwhile, a family of path planning algorithms address the problem of  
87 avoiding moving obstacles with field-based approaches. Regarding search-based algorithms, one of the  
88 most conventional yet still effective approaches for the navigation of an agent in a large map is related to  
89 Dijkstra and its extension of A\* searching algorithm (Cormen et al., 2009; Yershov and LaValle, 2011), and  
90 incremental search (Koenig et al., 2004b). In detail, the A\* algorithm improves the Dijkstra's algorithm  
91 by approximating the cost-to-go function with heuristic knowledge to reduce the searching space to the  
92 goal. Meanwhile, incremental search algorithms seek for the shortest paths by utilising the results of  
93 similar searches to make the search faster, instead of solving each search problem separately. By applying  
94 incremental search on top of the A\*, Koenig et al. (2004a) developed lifelong planning A\* (LPA\*) as an  
95 initial variant of A\*, in order to address path planning for dynamic graphs with changing edge costs. In the  
96 D\* algorithm (Stentz, 1994), incremental search is applied to repeatedly update the shortest paths between  
97 the current position of a robot and a goal, during the robot's approach to the goal. Koenig and Likhachev  
98 (2005) improved the D\* by LPA\* and alternatively Sun et al. (2009) developed dynamic fringe saving  
99 A\* to reuse the OPEN and CLOSED lists from previous A\* searches. Although different variants of A\*  
100 are able to address a graph change due to the moving of a robot to a new vertex, or the updates of edge  
101 costs, those algorithms still face difficulties to deal with moving obstacles. In addition, as stated by Hu and  
102 Brady (1997), a probabilistic approach is necessary to model the uncertainties of mobile obstacles in the  
103 environment. However, the complexity of path planning will be significantly increased if either the cost of  
104 the edges, or the links of the graph are presented by random variables.

105 In order to handle the uncertainties of observed obstacles, a field-based approach is another way to find  
106 the path for the agents. The field is calculated for each location, in time and space, and determines the  
107 directions of movement of an agent to reach the destination. The field consists of a repulsive field to push  
108 the agent away from the obstacles, and an attractive field to pull the agent towards the goal. For instance,  
109 Ok et al. (2013) proposed Voronoi uncertainty field which is build from Voronoi diagram from the start to  
110 the goal to create the attractive field and the repulsive field from the robot to the obstacles. The works of  
111 Wang and Chirikjian (2000) and later Golan et al. (2017) presented an artificial potential field based on the  
112 exchanges of heat flow. If obstacles are visualised as hot objects, the target is then presented as the cold one

113 and the temperature is discretised at each location on the grid. The temperature gradient solved by partial  
114 differential equation generates the appropriate forces to drive the robot. One of the big issues of using the  
115 potential field is that the repulsive field may push the agent to reach other obstacles or statures with the  
116 attractive field. Due to these problems, the agent may be trapped into a local optimum or loose its way  
117 toward the goal. To mitigate the local converge to a local optimal, some additions to the potential field have  
118 been introduced. Valbuena and Tanner (2012) proposed the way of adding velocity constraints, meanwhile  
119 García-Delgado et al. (2015) extended the repulsive function with the change of magnitude dependent  
120 on the angle between the attractive force and the obstacle. The main aim is to avoid the cancellation of  
121 the repulsive and attractive forces when applied in opposite orientations. However, the interactions of the  
122 agents with the environment, especially changes in the map, were not clearly addressed in above mentioned  
123 works. Besides, most of field-based navigation approaches lack the global information of a feasible path to  
124 the destination that could actually help avoid a trap that would lead to a local optimum.

125 Controlling the speed and directions of a robot are also key factors, which plays a role to provide the robot  
126 a collision free path. Owen and Montano (2005, 2006) defined velocity space to estimate the arrival time of  
127 moving objects to a region of potential collisions and thereby potential solutions to avoid these collisions.  
128 The velocity space in which the motion of the robot, as well as static and moving objects are mapped,  
129 is applied to predict when the collision may happen and when the robot may escape from the collision.  
130 Damas and Santos-Victor (2009) developed a map of forbidden velocity zones which is constructed as a  
131 limit on the velocity of the robot to avoid collision with obstacles. When the robot moves into the forbidden  
132 zones, it may adjust its speed to avoid the obstacles. Berg et al. (2008) Wilkie et al. (2009), and Berg  
133 et al. (2011) further integrated the acceleration while Lee et al. (2017) concerned the shape of the robots  
134 as an ellipse for obstacle avoidance. Yoo and Kim (2010) proposed a modified uni-vector field to present  
135 obstacles with respect to relative their velocities and positions where the gaze control which concerned the  
136 error of localisation and the distances to surrounding obstacles was also combined into the system to find  
137 the best moving trajectory. Belkhouche. (2009) introduced virtual plane to present moving objects with  
138 information of velocity into stationary ones. As a consequence, path finding in a dynamic environments  
139 is converted to a simpler problem of navigation in a static environment. However, it is noted that, it is  
140 not always optimal to use velocity planning when to drive the robot. Using only velocity control for path  
141 planning usually results in oscillatory motion. Given a typical differential drive mobile robot, there are  
142 a number of constraints on the linear and angular velocities, as well as the acceleration, in order to save  
143 energy for extending operation time, and finding the path to the goals with few turns. To the best of our  
144 knowledge, these concerns have not been investigated extensively in combination with obstacle avoidance  
145 in dynamic environment.

146 In order to address the above mentioned issues, in this paper, a novel method for path planning of mobile  
147 agents, in the shared working environment of human and agents, called as the dipole flow field, is proposed.  
148 The dipole flow field combines both global and local path planning in a unique framework. For global  
149 planning, the method applies any-angle path planning algorithm of Theta\* (Nash et al., 2010) to generate  
150 smooth paths with few turns, from a starting point to a goal for a pool of agents. Although different A\*  
151 variants of any-angle path planning haven been proposed, such as A\* post smoothing, block A\* (Yap et al.,  
152 2011) and field D\* (Ferguson and Stentz, 2006), the Theta\* is able to provide the most optimal path with  
153 simple and effective implementation (Uras and Koenig, 2015). As the computations of the Theta\* algorithm  
154 is costly for a big map, the algorithm is updated when there is a significant change on the static map of the  
155 environment. To cope with dynamic movements of the agents, a static flow field along the planned path  
156 is defined to attract the agent back to continue reaching the goal even when the agents may be deviated  
157 from the planned path. In addition, a dipole field is used to avoid the collision of the agents with others

158 and human within shared working space. To the best of our knowledge, most conventional approaches  
159 attempt to generate the pushing forces based only on the location of the agents, whereas in this work, it  
160 is assumed that, those should be better aligned with both moving directions and velocity magnitudes of  
161 different agents. The generated dipole field is able to push other agents far away based on their respective  
162 moving directions and the velocity magnitude of the agents. Static flow field and dipole field are combined  
163 to assure a dependable path of each agent from the starting point to the goal without colliding with each  
164 other.

165 The rest of paper is organised as follows. The methodology of the proposed path planning based on  
166 dipole flow field is presented in Section 2. The evaluation of the proposed method through the experimental  
167 results is described in Section 3. Finally, the paper is concluded with discussion in Section 4.

## 2 METHODOLOGY

168 In this section the agent architecture together with the different modules used for path planning are  
169 described in Section 2.1. Meanwhile the core path planning algorithm is presented in Section 2.2.

### 170 2.1 Autonomous Agent Architecture

171 The overall architecture of the autonomous agent to support the proposed planning algorithm is presented  
172 in Figure 1. The core algorithm includes the following five modules, *Map Generation*, *Path Initialisation*,  
173 *Static Flow Field Configuration*, *Collision Avoidance* and *Velocity Planning*. In addition, there are  
174 four external modules including *Sensor Data Collection*, *Update*, *Object Classification*, and *Movement*  
175 *Management* to help the planning algorithm collect information from the surrounding environment and  
176 update control.

#### 177 2.1.1 Path Planning Architecture

178 After that the global information of the environment is acquired from the external modules, a 2-D map  
179 is generated. The 2-D map is presented as a binary map in which static objects and obstacles are shown  
180 as black areas whereas the allowed moving areas are illustrated with white colour. Global path planning  
181 with Theta\* algorithm is applied in the *Path Initialisation* module to initiate a path from the starting point  
182 to the destination for the agents. While moving to the goal, the agent may deviate from the original path  
183 due to obstacle avoidance, or accumulated errors related to velocity and pose estimating. As a result, a  
184 static flow field generated in the *Static Flow Field Configuration* module will drive the agent back to the  
185 designed path. Only when the agent moves far away from the region covered by the static flow field, Theta\*  
186 is activated to renew the path from the current position to the goal. After the static flow field is configured,  
187 the agents start moving to reach their individual goals, while checking for collision with other moving  
188 objects. The dipole field is calculated in the *Collision Avoidance* module to avoid collision with the agents.  
189 Finally, the motions of the agents are controlled by the superposition of the static flow field, and dynamic  
190 dipole field to generate the dipole-flow force. The dipole-flow force is presented by the adjustments of the  
191 agents' heading angles. A velocity function is established to help the agent well adapt its moving velocity  
192 according to two factors, energy consumption and obstacle avoidance. If there is no collision, the agent will  
193 move with a stable speed along the configured path. Meanwhile, if there is a dynamic obstacle, the agent  
194 needs to adjust its moving direction to avoid the obstacle while still maintaining, or at least minimising, the  
195 deviation from the time to goal.

## 196 2.1.2 External Modules to Support Path Planning Algorithm

197 The *Sensor Data Collection* module is designed to continuously collect information of the environment.  
 198 For instance, the visual data obtained from a camera, together with the data from the other sensors, is used  
 199 to build the map of the environment and to recognise different objects. The pose of the robot is collected  
 200 from the inertial measurement unit (IMU). Similarly, the positioning tracking system registers the position  
 201 of the robot within the map. The *Object Classification* module receives the data from the *Sensor Data*  
 202 *Collection* module to determine which objects in the environment that are static objects and which ones are  
 203 moving objects. In this work, the proposed path planning algorithm deals with two types of moving objects.  
 204 Firstly, autonomous agents, which share information about their locations, and velocities, with the other  
 205 agents. Secondly, uncontrolled moving object, e.g. a human, who can suddenly appear in the working space  
 206 of the agents. Especially when the human subjects are present, the agents need to adjust their movement  
 207 to avoid them. The *Movement Management* module plays a central role in managing the location, and  
 208 moving trajectories of all agents and human(s) found in the environment. The data from the *Movement*  
 209 *Management* module is sent to the path planning algorithm for velocity estimation. The *Update* module  
 210 updates the internal model based on the changes in the environment, and applies the control commands  
 211 from the *Velocity Planning* module to move the agents accordingly.

## 212 2.2 Path Planning with Dipole Flow Field

213 In this section, the dipole flow field is firstly formulated by the combination of the static flow field and  
 214 the dynamic dipole field. Later, the direction of the dipole flow field at every point is turned into velocity  
 215 planning to control the linear and angular velocities of agents.

### 216 2.2.1 Static Flow Field for Global Path Planning

217 The global path consists of a sequence of line segments from the start to the goal, and is configured using  
 218 the Theta\* algorithm. Within the neighbourhood of the found path, a navigation field parallel to the path  
 219 segment, is defined, as the static flow field.

#### 220 2.2.1.1 Path Initialisation

221 To initialise the path from a starting point to an ending point, the Theta\* algorithm is applied. This algorithm  
 222 improves A\* by adding a line-of-sight (LOS) detection to each search iteration to find a less zigzaggy  
 223 path than those generated by A\* and its other variants. The primary difference between the Theta\* and the  
 224 others is that the Theta\* algorithm determines the parent of a node to be any node in the searching space.  
 225 Thence, the LOS detection feature is purposed to help decrease the undesired expanding by checking for  
 226 whether the offspring node and the parent are in a straight line, i.e. line-of-sight. By this means, the path  
 227 found by Theta\* is not a connection of adjacent nodes but a connection of line-of-sight ones. The pseudo  
 228 codes of the Theta\* is described in Algorithm 1.

229 As a heuristic-based search algorithm, Theta\* approximates the length of the shortest path based on  
 230 cost evaluation. The cost evaluation is conducted from the  $f$ -value, i.e. the lowest cost from the starting  
 231 node to the last node,  $s$ , in a path, referred to as  $f(s)$ , and a heuristic value called  $h$ -value which is the  
 232 cost estimation from the node  $s$  the goal. The estimated cost of the cheapest node through node  $s$  is, thus  
 233 expressed by

$$f(s') = f(s) + h(s, s'). \quad (1)$$

234 In this work, the heuristic function is simply defined as the Euclidean distance i.e.,  $h(s, s') =$   
 235  $w \cdot \text{Euclidean}(s, s')$  where  $w$  is a weight that determines the size of the area to search for the optimal

**Algorithm 1** Theta\* algorithm

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1: procedure THETA*( $s_{start}, s_{goal}$ ) ▷ Find the shortest path from start to goal location
2:    $open \leftarrow \emptyset$  ▷ To speed up Theta*,  $open$  is implemented with a priority queue
3:    $closed \leftarrow \emptyset$ 
4:    $g[s_{start}] \leftarrow 0$ 
5:    $parent[s_{start}] \leftarrow s_{start}$ 
6:    $open.insert(s_{start}, g[s_{start}] + h[s_{start}])$ 
7:   while  $open \neq \emptyset$  do
8:      $s \leftarrow open.pop()$ 
9:     if  $s = s_{goal}$  then
10:      return "path found" ▷ The found path is stored in  $parent[]$ 
11:    end if
12:     $closed \leftarrow closed \cup \{s\}$ 
13:    for  $s' \in neighbor(s)$  do
14:      if  $s' \notin closed$  then
15:         $g[s'] \leftarrow \infty$ 
16:         $parent[s'] \leftarrow NULL$ 
17:      end if
18:       $g_{old} \leftarrow g[s']$ 
19:       $COSTEVALUATION(s, s')$ 
20:      if  $g[s'] < g_{old}$  then
21:        if  $s' \in open$  then
22:           $open.remove(s')$ 
23:        end if
24:         $open.insert(s', g[s'] + h[s'])$ 
25:      end if
26:    end for
27:  end while
28:  return "no path found"
29: end procedure
30:
31: procedure COSTEVALUATION( $s, s'$ ) ▷ LOS check between  $parent[s]$  and  $s'$ 
32:  if  $LOS(parent[s], s')$  then
33:    if  $f(parent[s]) + h(parent[s], s') < f[s']$  then
34:       $parent[s'] \leftarrow parent[s]$ 
35:       $f[s'] \leftarrow f(parent[s]) + h(parent[s], s')$ 
36:    end if
37:  else
38:    if  $f[s] + h(s, s') < f[s']$  then
39:       $parent[s'] \leftarrow s$ 
40:       $f[s'] \leftarrow f[s] + h(s, s')$ 
41:    end if
42:  end if
43: end procedure

```

---

236 path around the straight-line between  $s$  and  $s'$ . With  $w > 1$ , Theta\* is able to reduce the searching area  
237 but may return a longer path, therefore the value  $w = 1$  is used in this work to search for the shortest  
238 path. It is assumed that the straight line distance between two nodes would never be longer than any other  
239 path connecting them. However, the shortest path generated by the A\* algorithm is connected by the  
240 neighbouring grid nodes, and thus entails many turning points to the robot. The path found by Theta\* is  
241 a sequence of LOS nodes so that it is smoother with few turns and closer to a straight-line path between

242 the start and the goal. The algorithm for LOS function is implemented with a drawing-line algorithm in  
243 graphics to optimise processing time and is referred to approach proposed by Nash et al. (2010).

244 As mentioned in Section 2.1.1, the input to the Theta\* algorithm is the binary map of the environment  
245 (Figure 2A). However, to avoid searching the path on a dense graph, a grid-based graph is used (as  
246 visualised in Figure 2B). The obstacle areas are also dilated corresponding to the size of agents so that the  
247 path found by Theta\* will not cause the boundary of the agent touching the edges of the map while the  
248 agent is moving.

### 249 2.2.1.2 Path Configuration with Static Flow Field

250 Searching for a global path from a start to a goal in a big map is a computationally heavy task, thus it is not  
251 desired to re-calculate the path for small updates of the map, or small deviations from the configured path.  
252 The static flow field is to draw the agents back to their moving paths in those situations. In the form of force  
253 interaction, the static flow field is also easily combined with a dynamic field for obstacle avoidance. As the  
254 shortest path found by Theta\* is the connection of several line segments, the static flow field is created  
255 within the neighbour of the line segments. For each path, it is assumed that there are  $n$  line segments from  
256 the start to the end points. Each line segment  $i$  is presented in a vector form of  $\mathbf{x}(t) = \mathbf{a}_i + t\mathbf{n}_i$  where  $\mathbf{a}_i$  is  
257 the starting of the line segment and  $\mathbf{n}_i$  is the unit vector of the line. To ensure that the static flow field will  
258 draw the agent to its goal, those line segments also includes the last line segment with  $\mathbf{a}_i$  is set to the goal  
259 and  $\mathbf{n}_i$  to a zero vector. The flow field force at the point  $\mathbf{p}$  close to the provided path found by Theta\* is  
260 calculated by

$$F_{flow}(\mathbf{p}) = F_a(\mathbf{p}) + F_r(\mathbf{p}) \quad (2)$$

261 where  $F_a(\mathbf{p})$  is the attractive force to draw agent back to the configured path, and  $F_r(\mathbf{p})$  is the repulsive  
262 force from nearby static obstacles. The configuration of the global path and the formulation of the flow  
263 force are described in Figures 3.

264 Let  $F_{a_i}(\mathbf{p})$  be the attractive force of a point to each line segment and expressed by

$$F_{a_i}(\mathbf{p}) = (1 - e^{-k_1 d(\mathbf{p}, \mathbf{a}_i)})((\mathbf{a}_i - \mathbf{p}) - ((\mathbf{a}_i - \mathbf{p}) \cdot \mathbf{n}_i)\mathbf{n}_i) + k_2 e^{-k_1 d(\mathbf{p}, \mathbf{a}_i)} \mathbf{n}_i \quad (3)$$

265 where  $d(\mathbf{p}, \mathbf{a}_i)$  is the distance from the point  $\mathbf{p}$  to the line segment  $i$ -th,  $k_1, k_2$  are constants, and " $\cdot$ "  
266 denotes the inner product of two vectors. As  $\mathbf{n}_i$  is a unit vector, the vector  $(\mathbf{a}_i - \mathbf{p}) - ((\mathbf{a}_i - \mathbf{p}) \cdot \mathbf{n}_i)\mathbf{n}_i$  is  
267 normalized before (3) is calculated. Two constants  $k_1 = 0.01$  and  $k_2 = 1$  are selected to control the impact  
268 of the first and second terms of equation (3). The attractive force  $F_a(\mathbf{p})$  is set equal to the attractive force  
269  $F_{\mathbf{a}_i^*}$  of the line segment  $\mathbf{a}_i^*$  closest to the point  $\mathbf{p}$ ,  $\mathbf{a}_i^* = \underset{\mathbf{a}_i}{\operatorname{argmin}} d(\mathbf{p}, \mathbf{a}_i)$ . Meanwhile, the repulsive force  
270  $F_r(\mathbf{p}) = -\nabla U_{rep}(\mathbf{p})$  is the negative gradient of the repulsive field

$$U_{rep}(\mathbf{p}) = \begin{cases} \eta \left( \frac{1}{d(\mathbf{p}, \mathbf{p}_0)} - \frac{1}{d_0} \right)^2 & d(\mathbf{p}, \mathbf{p}_0) \leq d_0 \\ 0 & d(\mathbf{p}, \mathbf{p}_0) > d_0 \end{cases} \quad (4)$$

271 in which  $d(\mathbf{p}, \mathbf{p}_0) = \|\mathbf{p} - \mathbf{p}_0\|$  is the Euclidean distance from the agent's position  $\mathbf{p}$  to the closest obstacle's  
272 position  $\mathbf{p}_0$ ,  $d_0$  is the influence distance of the force, and  $\eta$  is a positive constant. To avoid singularities  
273 of equation (4) when  $d(\mathbf{p}, \mathbf{p}_0) = 0$ , a linear transformation  $f(d) = \kappa d + 1$  is applied to map  $d(\mathbf{p}, \mathbf{p}_0)$   
274 and  $d_0$  to non-zero values  $f(d(\mathbf{p}, \mathbf{p}_0))$  and  $f(d_0)$  in equation (4). The influence distance of the force,  $d_0$ ,  
275 is selected based on the size of agents (the diameter of agents) to prevent touching the agents to static  
276 obstacles. With respect to  $0 < d_0 < 100$ ,  $\kappa = 0.01$  and  $\eta = 10^4$  are chosen. An example of repulsive field

277 of the binary map given in Figure 2A,B is shown in Figure 2C. The static flow fields without and with  
278 added repulsive forces are presented in Figure 4A and Figure 4B respectively.

279 The affecting area of the static flow field is determined by the window size ( $W$ ). This means that the  
280 static flow field remains influence on the agent if the distance from the agent to the designed path is less  
281 than  $W$ . Once the agent moves out of the affecting area, the Theta\* algorithm needs to be recalculated to  
282 update a new static flow field.

## 283 2.2.2 Dynamic Dipole Field

284 To cope with the problem of collision avoidance, the dipole field for each dynamic object is generated.  
285 The development of the dipole field is inspired by the way that humans naturally avoid moving obstacles:  
286 When facing an obstacle that is approaching, the human may turn, and continue to move, to avoid the  
287 obstacle instead of going backwards. Such a movement shows a moving trajectory similar to that of a dipole  
288 magnetic field line. This method is also a more skillful obstacle avoidance strategy than the conventional  
289 method of using radial potential field. Munasinghe et al. (2005) introduced an implementation of this  
290 obstacle avoidance method by designing a force to drive a robot through an elliptical trajectory to go around  
291 and then behind obstacles. In the work of Igarashi et al. (2010) the dipole characteristics is expressed as a  
292 vector field to push an object to a goal. In this work, to model the moving behaviour of agents, instead of  
293 developing dipole-like vector field the theory of dipole magnetic field in physics is directly applied. Each  
294 agent can be seen as a source of a magnetic dipole field, in which the magnetic moment is proportional to  
295 the velocity vector of the agent. This means that the orientation of the moment is aligned with the moving  
296 direction of the agent and the magnitude of the moment is equal to the speed of the agent. The aim of  
297 having the moment proportional to the speed is to ensure that among different obstacles having the same  
298 distance to the agent, the one with the larger speed will contribute a stronger effect on driving the agent.

299 In physics, the magnetic field  $\mathbf{M}$  of the dipole moment vector  $\mathbf{m}$  is expressed by

$$\mathbf{M}(\mathbf{m}, \mathbf{d}) = \rho(3(\mathbf{m} \cdot \hat{\mathbf{d}})\hat{\mathbf{d}} - \mathbf{m})/d^3 \quad (5)$$

300 where  $\mathbf{d}$  is the distance vector,  $d = \|\mathbf{d}\|$  is distance between two agents, and  $\hat{\mathbf{d}} = \mathbf{d}/\|\mathbf{d}\|$  is a unit vector.  
301 The magnetic constant  $\rho = 1/3$  ( $3\rho = 1$ ) is applied in this work instead of using  $\rho = \frac{\mu_0}{4\pi}$  in electromagnetic  
302 theory ( $\mu_0$  is the permeability of free space). An agent with the magnetic moment  $\mathbf{m}_j$  within the magnetic  
303 field  $\mathbf{M}_k$  generated by the other magnetic source  $\mathbf{m}_k$  would be affected by the force

$$\mathbf{F} = \nabla \mathbf{m}_j \cdot \mathbf{M}_k \quad (6)$$

304 where the gradient  $\nabla$  presents the changes of the quantity  $\mathbf{m}_j \cdot \mathbf{M}_k$  per unit distance. Hereby, the repulsive  
305 force of an agent  $k$  on an agent  $j$  can be formulated by,

$$\begin{aligned} \mathbf{F}_{dipole}(\mathbf{m}_j, \mathbf{m}_k, \mathbf{d}) &= \rho \nabla \left( \mathbf{m}_j \cdot \frac{3(\mathbf{m}_k \cdot \hat{\mathbf{d}})\hat{\mathbf{d}} - \mathbf{m}_k}{d^3} \right) \\ &= \rho \nabla \left( \frac{3(\mathbf{m}_j \cdot \mathbf{d})(\mathbf{m}_k \cdot \mathbf{d})}{d^5} - \frac{(\mathbf{m}_j \cdot \mathbf{m}_k)}{d^3} \right) \quad (7) \\ &= \rho \left( 3(\mathbf{m}_j \cdot \mathbf{d})(\mathbf{m}_k \cdot \mathbf{d}) \nabla \frac{1}{d^5} + \frac{3(\mathbf{m}_j \cdot \mathbf{d})}{d^5} \nabla (\mathbf{m}_k \cdot \mathbf{d}) + \frac{3(\mathbf{m}_k \cdot \mathbf{d})}{d^5} \nabla (\mathbf{m}_j \cdot \mathbf{d}) - (\mathbf{m}_j \cdot \mathbf{m}_k) \nabla \frac{1}{d^3} \right) \\ &= \frac{3\rho}{d^4} \left( (\mathbf{m}_j \cdot \hat{\mathbf{d}})\mathbf{m}_k + (\mathbf{m}_k \cdot \hat{\mathbf{d}})\mathbf{m}_j + (\mathbf{m}_j \cdot \mathbf{m}_k)\hat{\mathbf{d}} - 5(\mathbf{m}_j \cdot \hat{\mathbf{d}})(\mathbf{m}_k \cdot \hat{\mathbf{d}})\hat{\mathbf{d}} \right) \end{aligned}$$

306 where  $\mathbf{m}_j$ , and  $\mathbf{m}_k$  are the dipole moments of the agents. To lead to equation (7), the gradients of two  
307 functions,  $\nabla \frac{1}{d^n} = -n \frac{\mathbf{d}}{d^{n+2}}$  and  $\nabla(\mathbf{m} \cdot \mathbf{d}) = \mathbf{m}$ , are used.

308 The magnetic force  $\mathbf{F}_{dipole}(\mathbf{m}_j, \mathbf{m}_k, \mathbf{d})$  is aligned with the direction of from  $\mathbf{m}_k$  to  $\mathbf{m}_j$  to generate  
309 repulsive forces. This means  $\mathbf{F}_{dipole}(\mathbf{m}_j, \mathbf{m}_k, \mathbf{d})$  will be reversed if it has an opposite direction of a vector  
310 pointing from an agent  $k$  to an agent  $j$ . In order to increase the interaction range of dipole field, an  
311 adjustment factor  $\gamma$ ,  $0 < \gamma \leq 1$  and close to one ( $\gamma \approx 1$ ), is added as follows,

$$\mathbf{F}_{dipole}(\mathbf{m}_j, \mathbf{m}_k, \mathbf{d}) = \frac{3\rho}{d^{4\gamma}} \left( (\mathbf{m}_j \cdot \hat{\mathbf{d}})\mathbf{m}_k + (\mathbf{m}_k \cdot \hat{\mathbf{d}})\mathbf{m}_j + (\mathbf{m}_j \cdot \mathbf{m}_k)\hat{\mathbf{d}} - 5(\mathbf{m}_j \cdot \hat{\mathbf{d}})(\mathbf{m}_k \cdot \hat{\mathbf{d}})\hat{\mathbf{d}} \right). \quad (8)$$

312 The smaller value  $\gamma$  is, the further distance the dipole field of one agent has influence on the others. In  
313 addition, a small term  $\epsilon = 10^{-12}$  is added into  $d$  in the denominator of equation (8) to avoid singularities.

### 314 2.2.3 Dipole Flow Field

315 An agent needs to adjust its moving path according to its relative locations and orientations to other agents.  
316 Also, the agent concerns the possible collisions with uncontrolled moving objects i.e, humans, which does  
317 not share information about their locations, and intentions regarding how they will move. Assume that there  
318 are a set of  $N$  agents, i.e. robots  $\mathcal{A} = \{j | j \in 1, 2, \dots, N\}$  in the working space. All agents are designed  
319 using the same architecture to cooperate with each other to plan global movements so that each of them  
320 transmits location information to the other agents in  $\mathcal{A}$ . Let  $\mathcal{O}_j = \{o_j | o_j \in 1, 2, \dots, N_j\}$  be a set of  $N_j$   
321 human subjects recognised by the agent  $j$  within its detecting range. In this context, the relative location  
322 and velocity information about human subjects are estimations from observations over time. The dipole  
323 flow field for an agent  $j$  is formulated by integration of the static flow field, and the dynamic dipole field as

$$\mathbf{F}_{df}^{(j)} = \alpha \mathbf{F}_{flow}^{(j)} / \|\mathbf{F}_{flow}^{(j)}\| + \beta_A \sum_{k \in \mathcal{A}, k \neq j} \mathbf{F}_{dipole}(\mathbf{m}_j, \mathbf{m}_k, \mathbf{d}_{jk}) + \beta_O \sum_{l \in \mathcal{O}_j} \mathbf{F}_{dipole}(\mathbf{m}_j, \mathbf{m}_l, \mathbf{d}_{jl}) \quad (9)$$

324 where  $\|\mathbf{F}_{flow}^{(j)}\| = \sqrt{(\mathbf{F}_{flow}^{(j)x})^2 + (\mathbf{F}_{flow}^{(j)y})^2}$  is the magnitude of the flow force  $\mathbf{F}_{flow}^{(j)} = [F_{flow}^{(j)x}, F_{flow}^{(j)y}]^T$ ,  
325 here  $\alpha$ ,  $\beta_A$ , and  $\beta_O$  are constants. Those constants determine the impact of dipole flow forces over static  
326 flow forces to control the moving of agents. Since the static flow force is normalised in equation (9), the  
327 coefficient  $\alpha > 0$  represents for the magnitude of the static flow field term. To simply reflect the effective  
328 area of the static flow field,  $\alpha = 10$  is chosen (correspondent to the agents' diameter of  $1m$ , or 10 pixels, in  
329 all experiments). Meanwhile, the dipole field coefficients,  $\beta_A$  and  $\beta_O$ , determine the effecting area of the  
330 dipole field. It is able to define this area of influence of the agent ( $k$ ) on ( $j$ ) by a circle  $\mathcal{C}_{jk}$  that has a center  
331 at the agent ( $k$ ) and a radius  $r_{jk}$  to ensure that if  $d_{jk} < r_{jk}$  then  $\beta_A \|\mathbf{F}_{dipole}(\mathbf{m}_j, \mathbf{m}_k, \mathbf{d}_{jk})\| > \alpha$ . As the  
332 magnitude of  $\|\mathbf{F}_{dipole}(\mathbf{m}_j, \mathbf{m}_k, \mathbf{d}_{jk})\|$  is proportional to  $1/d_{jk}^{4\gamma}$ , the dipole forces has strong influence on  
333 the agent ( $j$ ) when the agent is inside  $\mathcal{C}_{jk}$ . On the contrary this influence is significantly decreased outside  
334  $\mathcal{C}_{jk}$ . In this work, the two constants  $\beta_A$  and  $\beta_O$  are set to be equal ( $\beta_A = \beta_O$ ) and defined to control the  
335 desired effective area of the dipole field. This area has a radius that is proportional to  $(\beta_A/\alpha)^{-1/4\gamma}$  and to  
336 the magnitude of dipole moments of agents. It is also noted that two agents ( $j$ ) and ( $k$ ) receives the dipole  
337 forces with the same amplitude but with opposite directions. Only agents are affected by the dipole forces  
338 generated by human subjects. Thus, in the model human subjects are not subject to these forces.

### 339 2.2.4 Velocity Planning

In this work, an autonomous agent is presented by the kinematics model of a unicycle-type mobile robot  
(Morin and Samson, 2008). This model is chosen because despite its unicycle name, it approximates

many widely used differential drive robots and can be easily extended to car-like mobile robots with two parallel driven wheels. The state of a robot (Figure 5) is described by a set of triple parameters  $s(t) = [x(t), y(t), \theta(t)]^T$ , and  $\mathbf{r}(t) = [x(t), y(t)]^T$  are the coordinates,  $\theta(t)$  is the orientation with respect to the  $x$ -axis of the robot, and  $t$  is time. The state  $s(t)$  is updated for every interval  $\Delta t$  as

$$\begin{aligned}x(t + \Delta t) &= x(t) + u(t)\Delta t \cos \theta(t) \\y(t + \Delta t) &= y(t) + u(t)\Delta t \sin \theta(t) \\ \theta(t + \Delta t) &= \theta(t) + \omega(t)\Delta t\end{aligned}\tag{10}$$

where  $u(t)$  and  $\omega(t)$  are the linear and angular velocities of the agent respectively. Those velocities are computed by the following equation

$$\begin{aligned}u(t) &= k_u \tanh(\|\mathbf{r}(t) - \mathbf{r}_{goal}\|) \\ \omega(t) &= -k_\omega \left( \theta(t) - \arctan\left(\frac{F_{df}^y}{F_{df}^x}\right) \right),\end{aligned}\tag{11}$$

340 where  $k_u > 0$  and  $k_\omega > 0$  are two constant control gains. From this definition, the linear velocity  $u(t)$  is  
 341 about  $k_u$  while an agent is moving on its ways and decays to zero when it is closer to the goal. Therefore,  
 342  $k_u$  is set to the expected speed of agent. Meanwhile, the angular velocity  $\omega(t)$  is used to adjust the heading  
 343 angle  $\theta(t)$  of the agent to make the agent's orientation aligned with the direction of dipole field force  $\mathbf{F}_{df}$ .  
 344 By this, the dipole flow field mainly affects the angular velocity  $\omega(t)$  of the agent to drive it to the goal and  
 345 to avoid the static obstacles, and moving objects when they are close. The second coefficient,  $k_\omega$ , controls  
 346 how smooth the moving trajectory of the agent is and how fast the agent is able to adapt to the changes of  
 347 the dipole field force.

### 3 EXPERIMENTS

348 A number of experiments are conducted to validate the effectiveness of the proposed path planning  
 349 algorithm. Different with most of existing approaches which have focused on alternative aspects of local or  
 350 global path planning for a single agent, this work has developed a new promising framework to address  
 351 the navigation problems of multiple agents sharing working space with human. This also adds a new  
 352 dimension to existing solutions of robotics navigation with the definition of dynamic dipole field inspired  
 353 from electromagnetic physics and of the static flow field based on Theta\* algorithm. Thus, the main aim  
 354 of this section is to investigate on the characteristics of the proposed approach through various scenarios.  
 355 The starting point is an experiment with static flow field. This experiment shows how this field is able to  
 356 navigate agents to goals within the map of complicated static obstacles. The next experiment exploits the  
 357 benefit of dipole field to help agents avoid moving obstacles coming from different directions. Finally, a set  
 358 of experiments are conducted in order to evaluate how well the proposed path planning algorithm with the  
 359 combination of flow and dipole flow fields, i.e. dipole-flow field, both drive agents toward the goals, and  
 360 at the same time avoid collisions with moving objects. Data showing the agent-agent and human-agent  
 361 distances in the presence of the dipole-flow field is also shown as part of the last experiment.

#### 362 3.1 Static Flow Field

363 The aim of the static flow field is to convert the path found by Theta\* into a navigation field to avoid the  
 364 needs of running Theta\* for every update of the agent position, and also to allow a more robust integration

365 of the path planning with obstacle avoidance and velocity controls. Thus, only when the agent deviates  
 366 from its designated path, due to slow adaptation to follow the navigation field, the path is required to be  
 367 renewed using the Theta\* algorithm. Different examples of agent movements with static flow field are  
 368 shown (Figure 6). In most situations, like examples given in Figure 6A and Figure 6B, the agent approaches  
 369 the goals without the needs of renewing the shortest path to the goal. However, in a particular case where  
 370 the agent deviates from the designed path, Theta\* is reused to update the path to the goal (Figure 6C).

371 Different windows of the static flow field are evaluated. One hundred trials are attempted for each specific  
 372 value of the window. In this experiment, a binary map of  $50 \times 50 \text{ m}$  with a resolution of 10 pixels per meter  
 373 is used. Each agent is presented by a bounding circle with a radius of  $0.5 \text{ m}$  and has the speed of  $0.5 \text{ m/s}$   
 374 with  $k_w = 1.2$  ( $k_u$  is set to the speed of agents in all experiments). The influence distance  $d_0$  is set to 10  
 375 pixels (or one meter). For each trial, an agent moves from a starting point to a goal using only static flow  
 376 field with velocity control. Pairs of starting and ending locations are selected randomly in the map. The  
 377 results reveal that the bigger window is, the less number of running Theta\* the static flow field needs (Table  
 378 1). For the following experiments in Section 3.2 and Section 3.3, the window of two times of the agent size  
 379 ( $W = 2S$ ) is applied.

### 380 3.2 Dipole Flow Field for Crossing Scenarios of Two Agents

381 To analyse the behaviour of dipole flow field for obstacle avoidance, two simple scenarios, in which  
 382 two agents are crossing each other are chosen (Figure 7). In Scenario 1, one of the agent moves from  
 383 left to right and the other agent moves in the opposite direction. In Scenario 2, the first agent moves as  
 384 previously, whereas the other agent starts in a position approximately  $90^\circ$  to the first agent and moves from  
 385 the left-hand to the right-hand side similar to the first agent. The variation of the moving directions of  
 386 the two agents is also evaluated by validating different values of the heading angle of the second agent  
 387 ( $\phi = 0, \phi > 0$  and  $\phi < 0$ , as seen in Figure 7). The size of the agents is set to a bounding circle with a  
 388 radius of  $0.5 \text{ m}$  while the ratio  $\beta_A/\alpha = 5$  and the coefficient  $\gamma = 1$  are used. In both scenarios, the two  
 389 agents moves at the same speed of  $0.5 \text{ m/s}$  (with  $k_w = 4$ ) so that their path intersects in the middle of their  
 390 way. However, with the help of repulsive forces generated by dipole field, the two agents are able to avoid  
 391 the collisions (Figure 8). Besides, after a small deviation from the path, due to the dipole field interaction  
 392 the agents turn back directly to their original paths to continue their routes towards their goals. The distance  
 393 plots show that the minimum distance of two agents are remained above the agent's diameter (marked with  
 394 the green line at  $1.0 \text{ m}$ , in Figure 9), thus there are no collisions present in the presented cases.

### 395 3.3 Dipole Flow Field for Multi-Agent and Human-Agent Interaction

396 In the first part of this section, the behaviours of multiple agents within dipole-flow field are analysed. In  
 397 the second part, the comprehensive evaluation of the dipole-flow field with the appearances of both agents  
 398 and humans are preformed. Also, in the second part, the concluding experiment, which demonstrates the  
 399 behaviour of the agents in presence of human in a large and realistic area, is presented.

400 Four agents, positioned at different orientations with the same distance to the centre of the map, take part  
 401 in the first testing scenario (Figure 10). All agents are planned to cross the centre, and move towards their  
 402 goals symmetrical to their starting positions. The agents travel within a binary map of a size of  $50 \times 50$   
 403  $\text{m}$  with a resolution of 10 pixels per meter and with static obstacles so that the free-space of moving and  
 404 avoiding other moving objects is limited. Also, the way to reach the goal is narrowed down and there is  
 405 a traffic circle in the centre of the map. Each agent has a radius of  $0.5 \text{ m}$  and a moving speed of  $0.5 \text{ m/s}$   
 406 (with  $k_w = 4$ ). The quantitative measurement of obstacle avoidance (with  $\beta_A/\alpha = 5$  and  $d_0 = 25$ ) is given

407 by measuring the minimum distance among agents over time . The closest distance of two agents when  
408 they are moving if smaller than their size will reveal a collision between them.

409 As depicted in Figure 10A, using flow-field navigation all agents are able to reach their goals. However  
410 there are existing collisions between agents (1)-(4), (2)-(4), and (3)-(4) (Figure 12A) with regards to the  
411 agent's radius of  $0.5 m$ . With dipole-flow-field navigation, agents show ability to avoid possible collisions  
412 (Figure 12B). Finally, the control factor ( $\gamma$ ) in dipole-flow field is evaluated to show its effects on the  
413 trajectories of agents in Figure 10C and the results in Figure 12A. When  $\gamma < 1$  is used, the collisions are  
414 prevent in a better way by keeping the minimum distances among agents bigger. It is important to note that  
415 the trajectories of moving agents are visualised to not interfering with any static obstacles from the binary  
416 map.

417 In order to evaluate dipole-flow-field for human-agent interaction, Agents 2 and 4 are replaced by two  
418 human subjects, which move as their agent counterparts, without caring the conflicts with agents. The  
419 moving trajectories of Agents 1 and 3 are described in Figure 11. Again, the collisions between agents are  
420 eliminated when agents are routed by the forces generated by dipole-flow field.

421 Finally, a general assessment of the dipole flow field for agent-agent and human-agent interactions within  
422 a large and complex binary map of variations of static obstacles drawn from a real building is presented.  
423 There are five moving agents and three human subjects in this evaluation. The map represents a part of the  
424 floor of a real building (width and length =  $200 \times 200 m$  with the same resolution of 10 pixels per meter).  
425 All agents have a bounding circle with a radius of  $0.5 m$ , while  $\beta_A/\alpha = 50$ ,  $d_0 = 25$ , and  $\gamma = 0.95$  are  
426 applied with bigger values than those of the previous experiments to help agents prevent collision from a  
427 further distance. An example of moving trajectories of different agents with human is shown in Figure 13.  
428 The experiments were repeated 100 times, and for each trial start and goal positions of both agents and  
429 humans were randomised. The requirement for finding the start position and goals was that the pairwise  
430 distances among them should be at least  $2.0 m$ . The speed of the agents and human during the experiment  
431 is randomly assigned within a range of  $0.5 - 1.5 m/s$  using a uniform distribution (with  $k_\omega = 4$ ). For each  
432 trial, agent-agent and human-agent the distances are recorded for the evaluation purposes. The overall  
433 result is summarised in Table 2.

## 4 CONCLUSION AND DISCUSSION

434 This paper has introduced a novel path planning algorithm for agents surrounded by static and multiple  
435 moving objects, including other robotic agents as well as humans subjects, all populating a realistic working  
436 space. The algorithm is able to process path planning in real-time by developing a navigation field so that  
437 the movements of agents is just simply controlled by the forces generated from this field. The attractive  
438 forces that drive the agents toward their desired goals are created by a static flow field. Simultaneously, the  
439 repulsive forces that prevent agent-agent, and human-agent, collisions are generated by a magnetic field of  
440 dipoles. The combination of the static flow field and dipole field forms a force to determine the moving  
441 directions of the agents at a specific time instance.

442 The evaluation of the proposed approach with the static flow field, dipole field and their combinations are  
443 conducted with distinctive experiments. With static flow field, it is obvious that an agent is able to move  
444 to its goals in a binary map of static obstacles with a minimum number of re-initialising the global path  
445 using the Theta\* algorithm. As can be seen in Table 1, the number of running Theta\* instances except the  
446 first initiation is less than one time in average (if the window effects of the static flow field is set to at least  
447 twice the size of the agents,  $W \geq 2S$ ). However, an unnecessary large window may cover otiose areas that

448 affect the static flow field, leading to the trap of agent into a corner of the map. Therefore, the window size  
449  $W = 2S$  is recommended to increase the robustness of the static flow field and to avoid the possibility of  
450 local traps.

451 Within the combined dipole-flow field, the robotic agents are well routed to their destinations, while  
452 possible collisions with other agents and human are taken into account. Regarding overall evaluation of the  
453 dipole-flow field to navigate agents in a complex scenario, the average minimum distance between any two  
454 agents remains at least double the radius of bounding circle, which indicates that there are no collisions  
455 (Table 2). The minimum human-agent distance is  $1.0 m$ . However, such a recorded observation in which  
456 the human-agent distance is close to  $1.0 m$  is only one case in 1500 obtained distance pairs (there is a group  
457 of five agents and three human subjects in the experiment so that the obtained pairs of human-agent is 1500  
458 over 100 trials). Regarding the size of the human subjects, the bounding circle radius can be configured  
459 even less than  $0.5 m$ , therefore it can be concluded that no occlusions happen in any of the simulation runs.

460 Recently, the aim of this work has moved towards holistic navigation solutions in real-world problems  
461 more specifically, mobile robots in densely populated areas such as, offices, and heavy vehicles in restricted  
462 spaces. Thus, by adding a control mechanism for the velocity e.g., decreasing the speed to avoid possible  
463 collisions, as well as other measures will be investigated. Besides controlling the agents' velocity, the  
464 configuration of global paths with regards to multiple agents is also an important factor to ensure the  
465 reachability of all agents to their goals. In the current approach, only one optimal path to the goal is  
466 configured for each agent, without considering the conflicts with others. If any two agents enter into a  
467 very narrow area on opposite directions, as described by Kimmel and Berris (2016), the dipole forces  
468 mainly push them away to avoid collisions but not help them build new paths to their goals. Therefore,  
469 the two agents tend to follow the same planned paths again and again, leading to a deadlock situation.  
470 The proposed approach could be improved by setting multiple paths for each agent. Upon evaluating the  
471 location information of others and the binary map of environment, an agent is able to decide which path,  
472 even not optimal, it should follow to reach its goal. The aforementioned problem could be also addressed  
473 by exchanging information of planned paths among agents. All agents will negotiate to optimise the flow  
474 field on a global scale to avoid any deadlock situation. However, in this case the communication protocol  
475 will become more complicated and extra processing is needed at each agent side to optimise the global  
476 path with respect to the presence of other agents. Finally, the work will be extended with different classes  
477 of agents (Panagou, 2017), and with multiple heuristics of A\* (Aine et al., 2016) to allow more thoroughly  
478 investigation of the dependability factors, and constraints on the path planning problems. The intention is  
479 also to validate the algorithm using robots and humans in outdoor settings, that resemble the qualities of  
480 construction sites.

## CONFLICT OF INTEREST STATEMENT

481 The authors declare that the research was conducted in the absence of any commercial or financial  
482 relationships that could be construed as a potential conflict of interest.

## AUTHOR CONTRIBUTIONS

483 This work is based on the original idea proposed by Mikael Ekström, later developed by Lan Anh Trinh.  
484 Lan Anh Trinh, and Baran Cürüklü contributed to the design of experiments. All authors contributed to the  
485 development of system architecture and to the writing of the manuscript.

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## TABLE

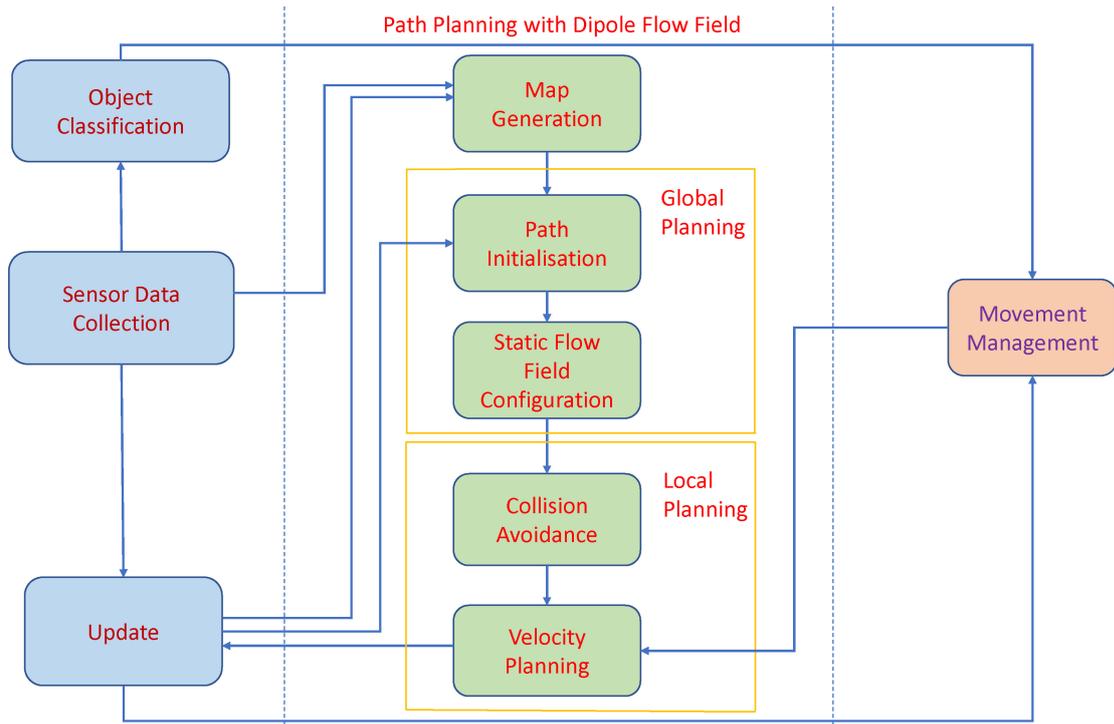
**Table 1.** Relationship between an average number of Theta\* used for static flow field to successfully drive an agent to its goal and window size ( $W$ ). (The size of an agent is  $S$ )

Window size	$W = S/4$	$W = S/2$	$W = S$	$W = 3S/2$	$W = 2S$	$W = 5S/2$
Average number of Theta*	10.85	4.57	1.53	0.73	0.43	0.23

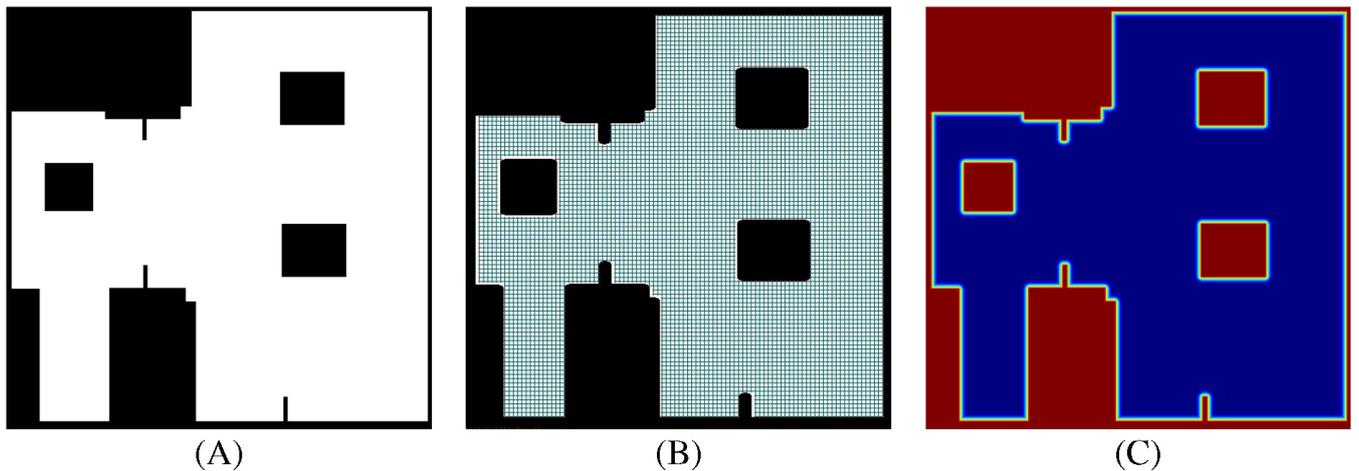
**Table 2.** Evaluation of the minimum, and average, of agent-agent and human-agent distances over all 100 trials.

Minimum of agent-agent distances ( $m$ )	Minimum of agent-human distances ( $m$ )	Average of minimum agent-agent distances ( $m$ )	Average of minimum agent-human distances ( $m$ )
2.4	1.0	10.0	8.8

## FIGURE



**Figure 1.** The Architecture of Autonomous agent. The backbone of the path planning algorithm consists of the *Map Generation* module, *Global Planning* including the *Path Initialisation* module and the *Static Flow Field Configuration* module, and *Local Planning* including the *Collision Avoidance* module and the *Velocity Planning* module.



**Figure 2.** Binary map for static flow field and derived information, (A) the original binary map in which the white pixel presents available regions of agents, (B) the grid-based graph derived from the binary map, and (C) the corresponding repulsive field in which the amplitude of the field from the lowest to the highest is mapped into colors from blue to red respectively.

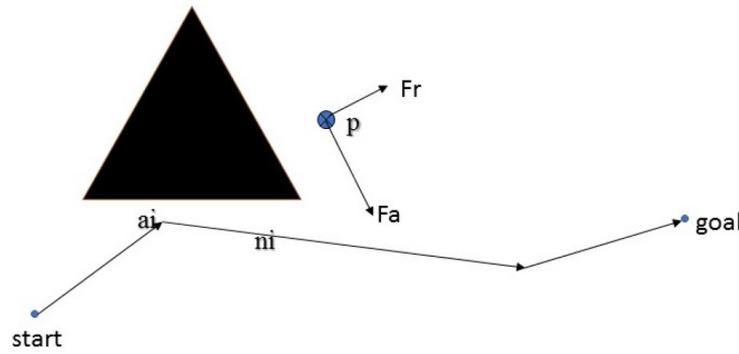


Figure 3. The configuration of the global path.

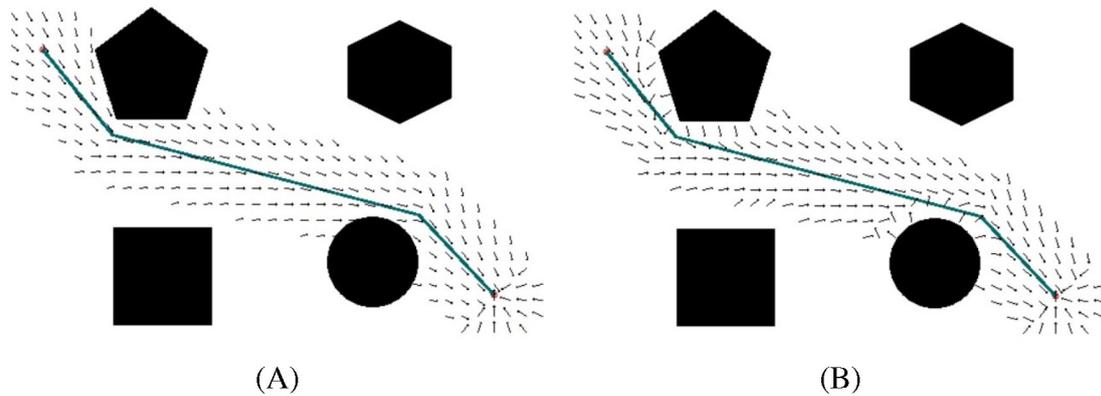


Figure 4. The representation of the static flow field (unity vectors), (A) the initial path with the configured static attractive field, (B) the static flow field with added repulsive force to the obstacles.

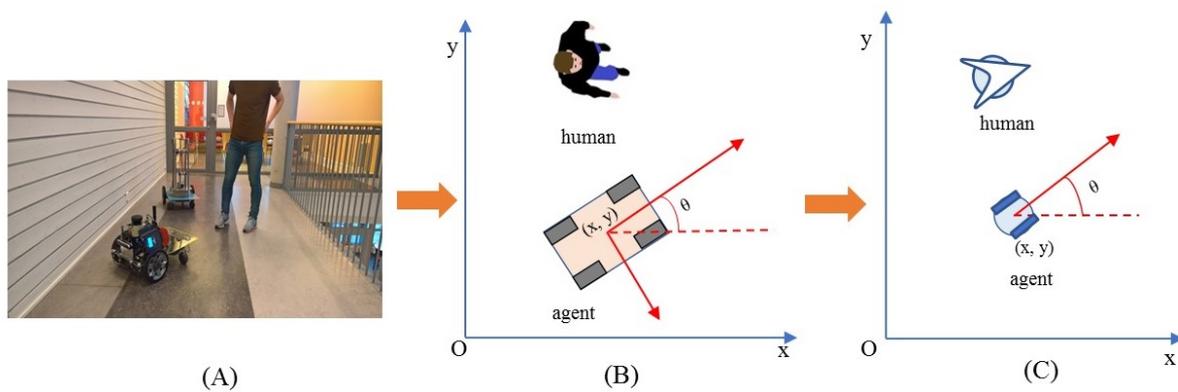
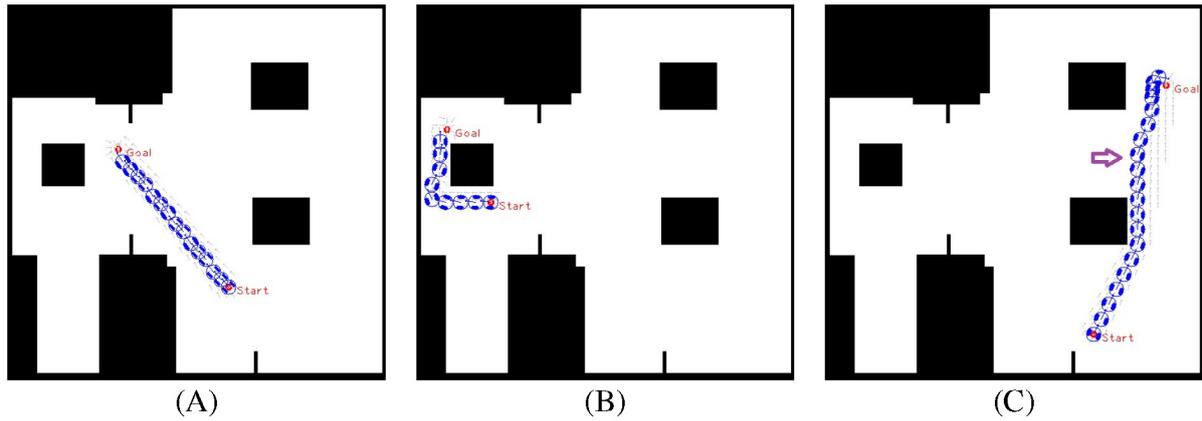
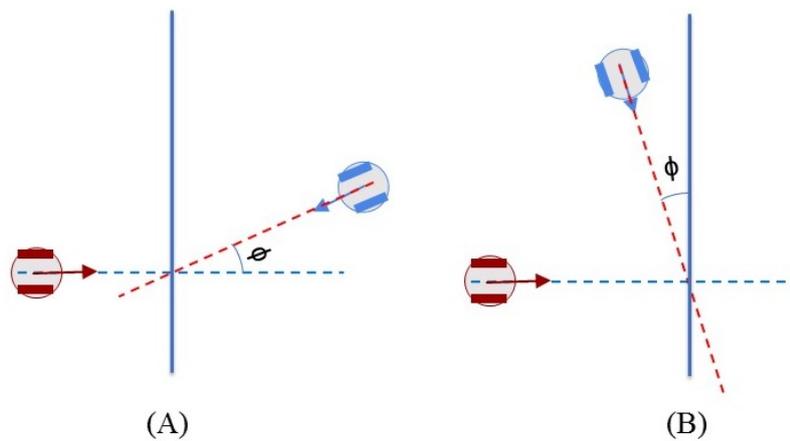


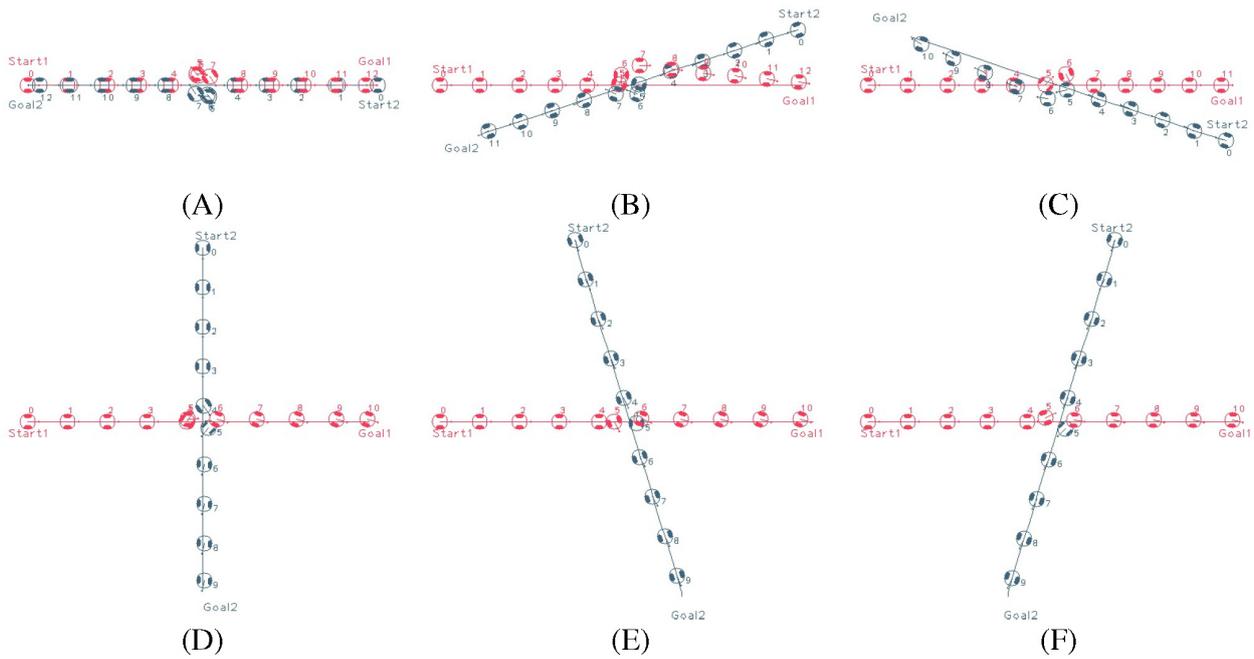
Figure 5. Visualisation of an agent with kinematic parameters and human from (A) a real world space in (B) a 2D mapping space, and (C) a simplified visualization used in the proposed work.



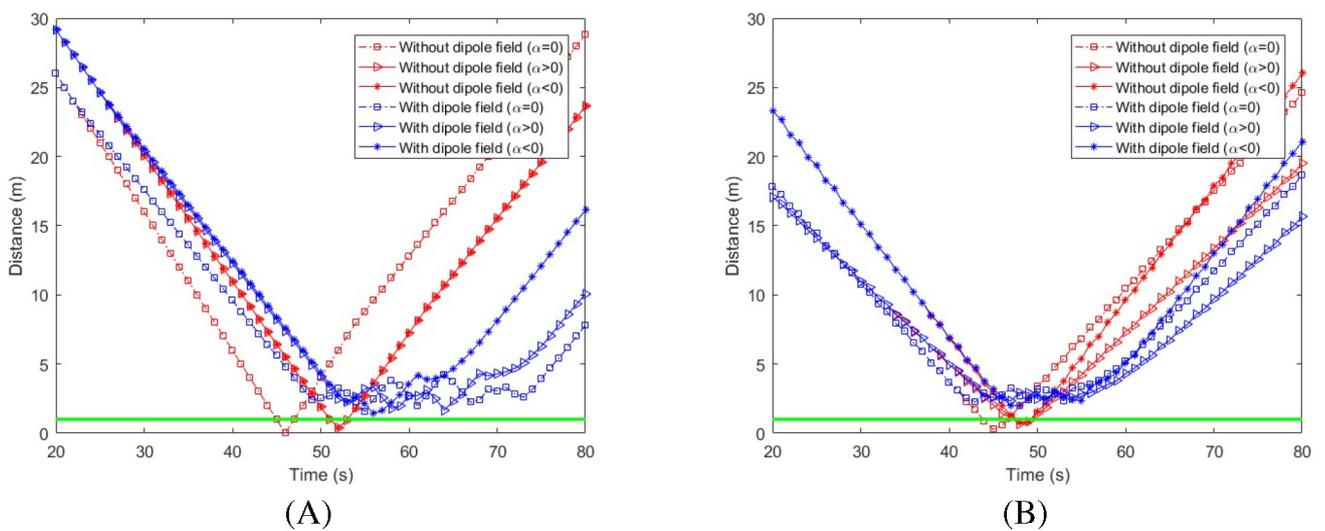
**Figure 6.** Agent moves from start to goal with static flow field where the window of static flow field is set as two times as the size of the agent. (A) and (B) an agent approaches the goal without the needs of re-estimating a new path, and (C)  $\Theta^*$  is reactivated when the agent gets close to the second obstacle along its path (the location for activation is shown by the arrow symbol).



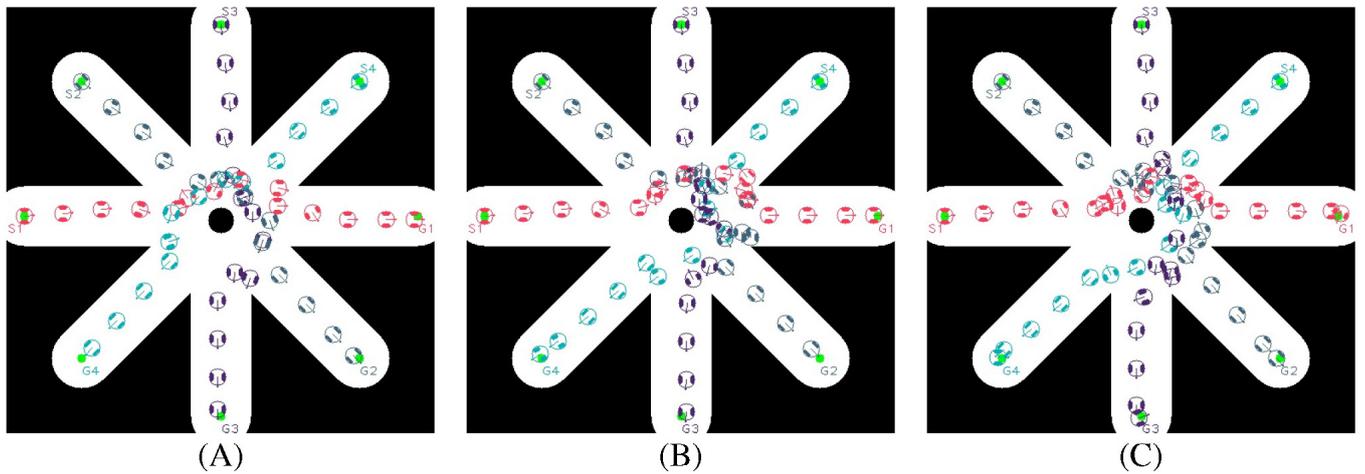
**Figure 7.** Crossing scenarios of two agents (A) Scenario 1: Two agents move toward each other with opposite directions and (B) Scenario 2: Two agents move toward each other with the heading angles of around  $90^\circ$ .



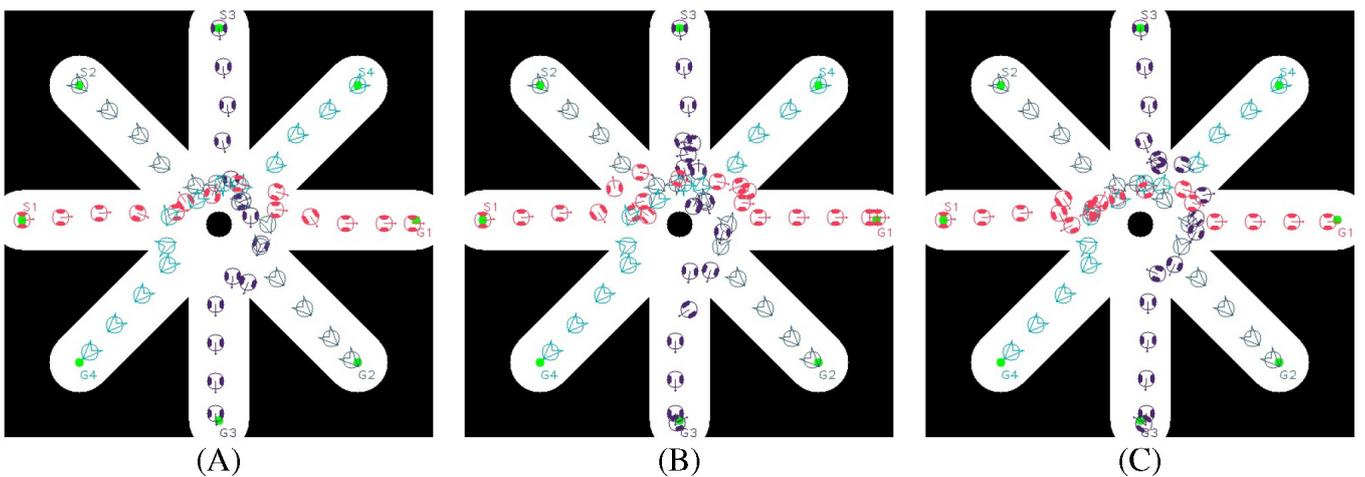
**Figure 8.** Trajectories of two agents in two scenarios. The first rows visualise the moving behaviors in dipole field of agents in Scenario 1 with different value of  $\phi$ , (A)  $\phi = 0$ , (B)  $\phi > 0$ , and (C)  $\phi < 0$ . Similarly, the second rows show the results of Scenario 2 with (D)  $\phi = 0$ , (E)  $\phi > 0$ , and (F)  $\phi < 0$ . The time indices are used to show the location of agents at every 10 seconds.



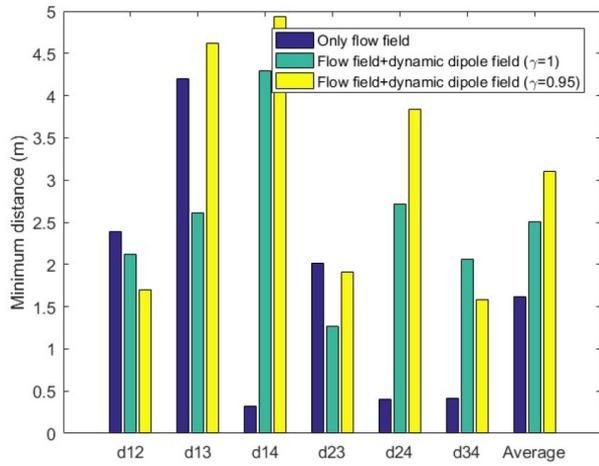
**Figure 9.** Distance of two agents over time in (A) Scenario 1 and (B) Scenario 2. The green baseline depicts the minimum distance between agents to avoid collisions.



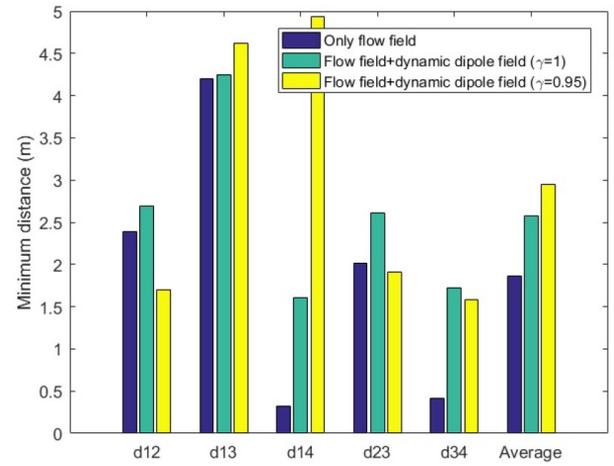
**Figure 10.** Trajectories of multiple agents moving (A) without dipole field, (B) with dipole field  $\gamma = 1$ , and (C) with dipole field  $\gamma = 0.95$ .



**Figure 11.** Trajectories of multiple agents moving and interacting with human (A) without dipole field, (B) with dipole field  $\gamma = 1$ , and (C) with dipole field  $\gamma = 0.95$ .

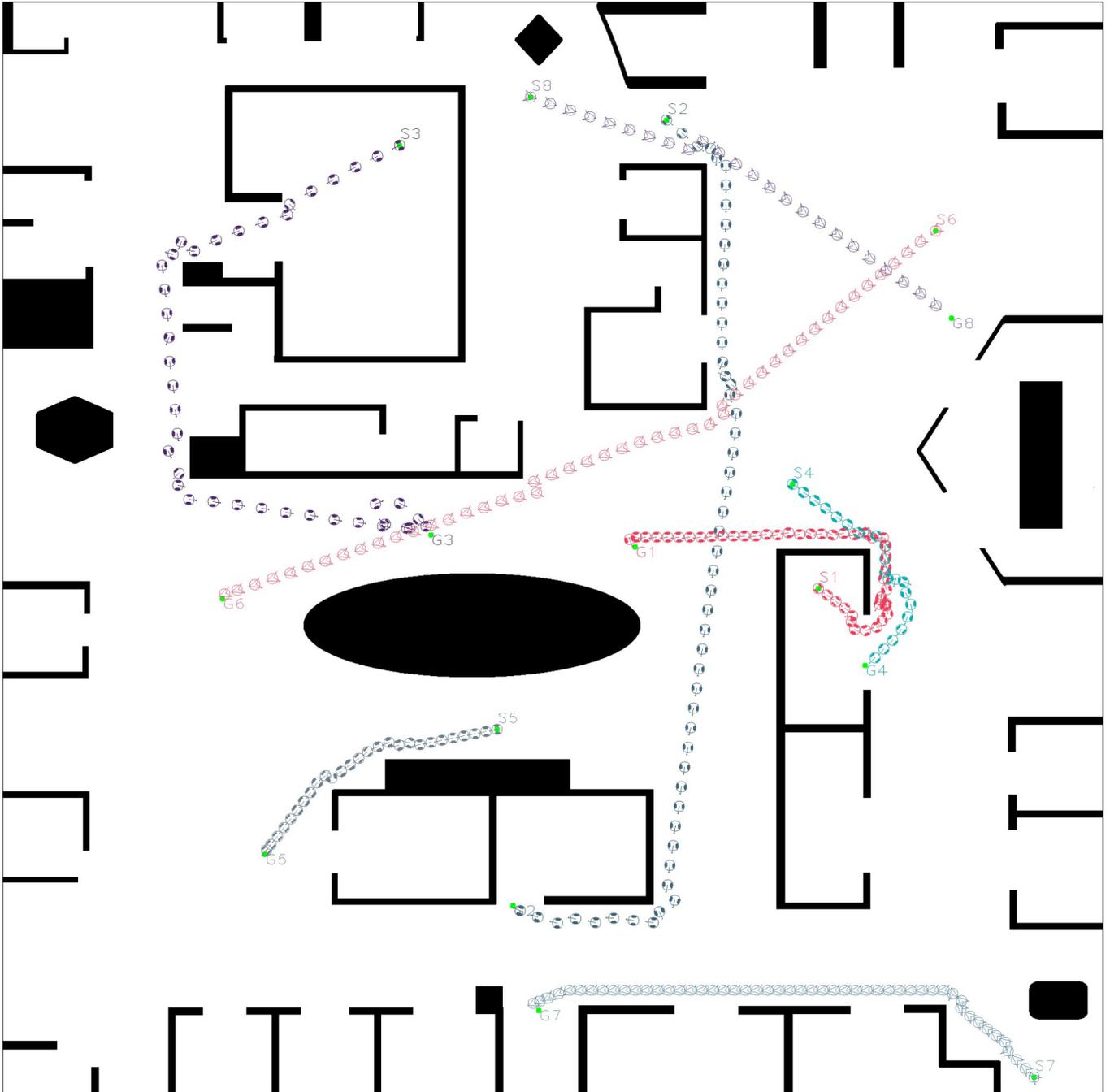


(A)



(B)

**Figure 12.** Minimum distance of agents over time in (A) multi-agent, and (B) human-agent interactions within dipole-flow field.



**Figure 13.** Dipole-flow field to control movements of multiple agents with the presence of three human in a  $200 \times 200 \text{ m}$  large map which is visualised from a real working space. All agents are able to reach their goals with different speeds. While moving to goals, the two agents with indices 2 and 3 try to avoid the collision with human with index 6. Meanwhile, two agents with indices 1 and 4 also change directions to avoid collision with each other. In the case of the agent with index 3, the goal  $G3$  is very close to the moving trajectory of human, therefore its way to the goal seems to be blocked until human with index 6 passes through  $G3$ . In consequence, the agent 3 must go back and later turn around to reach its goal. This behavior of moving is quite different with the scenario described in Figure 10B.