

# Designing Self-Adaptive Software Systems with Control Theory: An Overview

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**Abstract**—The complexity of modern software systems is continuously growing, as well as the amount of data that is produced on a daily basis. This calls for sound and scalable approaches that can be used to tame such an emerging complexity. This tutorial aims at introducing the basic concepts of control theory that can be used to design self-adaptive systems. The tutorial is divided into two main parts. The first part discusses the modeling of discrete-time systems, and the design of controllers in the discrete-time domain. The second part presents a number of successful examples of the application of control-based approaches for the design of self-adaptive software systems.

**Index Terms**—self-adaptive systems, control theory, software design

## I. INTRODUCTION AND MOTIVATION

The number of Internet of Things (IoT) devices is increasing exponentially, and it is expected to reach 31.4 billion by 2023 [1]. Digitalization and the Industrial IoT (IIoT) have caused business models to change, and many companies are increasingly becoming data companies, as they collect, administer, and analyze massive amounts of data to support their primary operations. IoT has gained a lot of attention in several areas including smart houses, industrial automation, and robotics, and applications are becoming more and more distributed, posing a number of challenges for the **management of the computational resources** needed for handling such increasingly complex systems, and for the **design of scalable and efficient solutions**.

The design of automated decision-making strategies for computing systems is known in the literature as **self-adaptation**, i.e., computing systems dynamically adapt to changes. Several disciplines have been identified as potential contributors. Among these, machine learning provides additional knowledge of the system [2], and control theory provides a vast array of tools for designing robust adaptive physical systems with formally assured behavior [3]. The combination of knowledge, robustness and formal guarantees has led to increased interest in developing control-based approaches to various computing system problems [4], [5].

Self-adaptation has a key role in the development of software systems [3] and control theory has proven to be a useful tool to introduce adaptation in such systems [5]–[10]. Self-management techniques are also prominent in the cloud industry. For example, companies like IBM (see projects like the

IBM Touchpoint Simulator, the K42 Operating System [11]), Oracle<sup>1</sup>, and Intel<sup>2</sup>.

The research area of applying control theory to computing systems is becoming quite vast, as also analyzed in the recent survey by Shevtsov et al. [12]. Developing accurate system models for computing systems is in fact hard [13]–[15]. Moreover, both expertise in the computing system to be modeled, along with mathematical modeling skills are needed to deal with real systems [16]. These difficulties usually lead to the design of controllers focused on particular operating regions or conditions and *ad hoc* solutions that address a specific computing problem using control theory, but do not generalize [17], [18]. For example, in [19] the specific problem of building a controller for a .NET thread pool is addressed.

This line of research is motivated by the belief that safe, reliable, and resource-efficient solutions will not be possible without a firm mathematical foundation. Being able to program and manage computing systems efficiently and autonomously, while providing guarantees on the runtime behavior is of fundamental importance. As a consequence, a deeper understanding of control theory, and how a control-based solution can be designed can be beneficial to software designers to build more efficient computing systems.

## II. TUTORIAL STRUCTURE

### A. Introduction to Discrete-time Control Systems

In the first part, the basic principles of linear control theory for discrete-time systems are revised [20], [21], including

- The introduction of the basic notation used in control systems, for the control input  $u(t)$ , the measured output  $y(t)$ , and the state variable  $x(t)$ . The variable  $t \in \mathbb{Z}$  counts the discrete time.
- The definition of a discrete-time linear time-invariant system in the state-space form

$$\begin{cases} x(t+1) = Ax(t) + Bu(t) \\ y(t) = Cx(t) + Du(t) \end{cases}$$

where the matrices have suitable sizes.

<sup>1</sup>Oracle Automatic Workload Repository: <https://oracle-base.com/articles/10g/automatic-workload-repository-10g>

<sup>2</sup>Intel RAS Technologies for Enterprise: <http://intel.ly/1TMzPKG>

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- An introduction of the discrete-time PID (Proportional Integral Derivative) control law in the *velocity form*,

$$\begin{aligned}
 u(k) &= u(k-1) \\
 &+ K_p (e(k) - e(k-1)) \\
 &+ K_i h e(k) \\
 &+ K_d \frac{e(k) - 2e(k-1) + e(k-2)}{h}
 \end{aligned}$$

and a discussion on how this can be implemented as a simple function in a software component.

- An introduction to more advanced control techniques, such as the Model Predictive Control (MPC) (more extensively presented in [21]).

## B. Application Examples

The tutorial will also explore in more detail different research results that have been developed over the years using such kinds of techniques. In particular, the presented examples are:

- Task scheduling in real-time systems [22], [23].
- Clock synchronization in wireless sensor networks [24]–[27].
- Control of cloud-based applications [28]–[31].
- Elastic data streaming applications [14], [15].

## C. Automating the design process

The tutorial concludes with the analysis of current trends in the area of software engineering for the automated design of control systems for self-adaptive software [32], [33], and some remarks on future research directions.

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